



Center for  
**LifeLong  
Learning  
& Design**

University of Colorado at Boulder

**Wisdom is not the product of schooling  
but the lifelong attempt to acquire it.  
- Albert Einstein**

**Solving Problems by Search**  
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**Chapter 3 in Russell / Norvig Book**

Gerhard Fischer

AI Course, Fall 1996, Lecture September 16

# Overview

- **problem solving agents:** goals, goal formulation, problem formulation
- **formulating problems:** knowledge and problem types, well- and ill-defined problems
- **example problems:** toy problems and real world problems, semantically poor and rich problems
- **searching for solutions:** generating action sequences, data structures for search trees
- **search strategies:** breath first, depth first, bi-directional search
- **avoiding repeated states:** record the states which have been visited
- **constraint satisfaction search:** states are defined by variables, goal test specifies a set of constraints

# Well-Defined versus Ill-Defined Problems

- **Well-Defined Problems:**
  - the essential conditions of the problem are stated
  - their solutions are the same for all problem solvers
  - examples: school problems, mutilated checker board, implementing given algorithms
- **Ill-Defined (or Wicked) Problems:**
  - problem solver takes an active role what the problem is
  - fill gaps in the problem definition
  - jump into the problem
  - use information gained while trying to solve the problem
  - examples: architects, engineers, lawyers, legislators, software, designers, writers, teachers, ....

# Semantically Rich Domains versus Semantically Poor Domains

- **“poor”**
  - knowledge in cryptarithmic problems: numbers, how to add and subtract, facts about parity
  - puzzles (missionaries and cannibals)
- **“rich”**
  - driving a taxi in a big city
  - medicine
  - law
  - using Unix, Word, Excel, .....(high functionality applications)
- **questions: what is**
  - chess
  - programming

# Problem Solving and Search — Cryptarithmic Problems

DONALD  
+ GERALD  
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ROBERT

D=5

CROSS  
+ ROADS  
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DANGER

- sophisticated strategy (= more knowledge) ----> less search
- brute force search:  $10! = 3,628,800$  possibilities
- with  $D = 5$  ---->  $9! = 362,880$

# Number Scrabble

- two person game
- nine cards: 1, 2, 3, 4, 5, 6, 7, 8, 9
- cards are placed face up
- players draw alternately, one at a time, selecting any of the remaining cards
- goal: to have drawn cards so three of them add up to 15 (before the opponent can do so)

# Tic-Tac Toe

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# Search Strategies

**completeness:** is the strategy guaranteed to find a solution when there is one?

**time complexity:** how long does it take to find a solution?

**space complexity:** how much memory does it need to perform the search?

**optimality:** does the strategy find the highest-quality solution when there are several different solutions?

**uninformed search:** no information about the number of steps or the path cost from the current state to the goal — all they can do: distinguish a goal state from a non-goal state

**informed search (or heuristic search):** use information, heuristics, guesses about the search space (chapter 4 in Russell / Norvig)



## Example Problem

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### Going from the Engineering Center to the Flagstaff House

- well-defined or ill-defined?
- breath-first search
- depth first search